

Final Exam Review Factors and Products

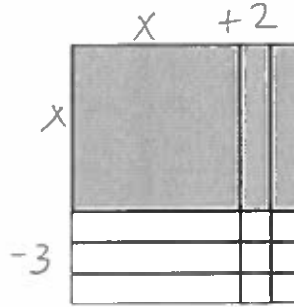
Section One: Circle the correct solution.

1. For the expression $x^2 - \boxed{?}x - 12$ to be factorable, give the value for $\boxed{?}$.
- (A) 2 (B) 3 (C) 4 (D) 6

12, 1
3, 4
-6+2

2. A polynomial is represented by the tiles shown below. What are the factors of the polynomial? (Consider the shaded tiles positive!!)

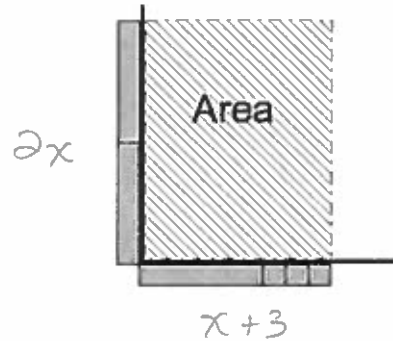
- (A) $(x + 3)(x - 2)$
 (B) $(x + 3)(x + 2)$
 (C) $(x - 3)(x - 2)$
 (D) $(x - 3)(x + 2)$



3. Two students set up some algebra tiles to help model a product. Which expression represents the modeled area? (Shaded tiles are positive)

- (A) $x^2 + 6x$
 (B) $2x^2 + 3x$
 (C) $x^2 + 3x$
 (D) $2x^2 + 6x$

$2x(x+3)$
 $2x^2 + 6x$



4. Multiply: $(2x - 3)(3x + 4)$. $= 6x^2 + 8x - 9x - 12 = 6x^2 - x - 12$

- (A) $6x^2 - x - 12$ (B) $6x^2 - 12$
 (C) $6x^2 - 17x - 12$ (D) $6x^2 + 2x - 12$

5. A rectangle has dimensions $(2x - 3)$ and $(3x + 1)$. Find the area of the rectangle.

- (A) $5x - 2$ (B) $6x^2 - 7x - 3$
 (C) $6x^2 + 7x - 3$ (D) $5x^2 - 7x - 3$

$(2x-3)(3x+1)$
 $= 6x^2 + 2x - 9x - 3$
 $= 6x^2 - 7x - 3$

6. Which is the product of $(x + 3)$ and $(3x - 2)$?

- (A) $3x^2 - 6$ (B) $4x^2 - 6$
 (C) $3x^2 + 7x - 6$ (D) $4x^2 + 7x - 6$

$(x+3)(3x-2)$
 $3x^2 - 2x + 9x - 6$
 $3x^2 + 7x - 6$

7. The area of a rectangle is $x^2 - 2x - 24$. What are the dimensions?

- (A) $(x + 4)$ by $(x - 6)$ (B) $(x - 4)$ by $(x + 6)$
 (C) $(x + 4)$ by $(x + 6)$ (D) $(x - 4)$ by $(x - 6)$

$= (x-6)(x+4)$

8. Factor completely: $4x^2 - 25$ $(2x-5)(2x+5)$
 (A) $(4x-25)(4x+25)$
 (B) $(2x-5)(2x-5)$
 (C) $(2x-5)(2x+5)$
 (D) $(2x+5)(2x+5)$

9. Factor completely: $2x^2 + 4x - 6$ $2(x^2 + 2x - 3)$
 (A) $(x+3)(x-1)$
 (B) $(2x-2)(x+3)$
 (C) $2(x^2 + 2x - 3)$
 (D) $2(x-1)(x+3)$

10. Expand and simplify: $(x+2)(2x^2 - x + 5)$ $= 2x^3 - x^2 + 5x + 4x^2 - 2x + 10$
 (A) $2x^3 + 3x^2 + 3x + 10$
 (B) $2x^3 - x^2 + 5x + 10$
 (C) $2x^3 + 5x^2 + 7x + 10$
 (D) $2x^3 + 3x^2 + 7x + 10$

Section Two: Answer all questions. You MUST show your work to get full credit.

1. Expand and simplify using the method of your choice.
 (A) $(2x-1)(x+3) - (3x+2)(2x+5)$
 (B) $(x^2 - 2x + 5)(2x^2 + 4x - 1)$

1. A. $(2x^2 + 6x - x - 3) - (6x^2 + 15x + 4x + 10)$
 $(2x^2 + 5x - 3) - (6x^2 + 19x + 10)$
 $2x^2 + 5x - 3 - 6x^2 - 19x - 10$
 $-4x^2 - 14x - 13$

2. Factor fully each of the following expressions:

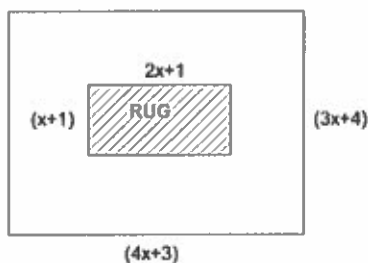
(A) $x^2 - 5x - 14$
 $(x-7)(x+2)$
 (B) $8x^2 + 10x - 3 = 8x^2 + 12x - 2x - 3$
 $= 4x(2x+3) - 1(2x+3)$
 $= (4x-1)(2x+3)$

1B. $2x^4 + 4x^3 - x^2$
 $- 4x^3 - 8x^2 + 2x$
 $+ 10x^2 + 20x - 5$
 $2x^4 + x^2 + 22x - 5$

(C) $6x^2 - xy - 2y^2$
 $6x^2 - 4xy + 3xy - 2y^2 = 2x(3x-2y) + y(3x-2y)$
 $= (2x+y)(3x-2y)$

(D) $81x^4 - 16y^4$
 $(9x^2 - 4y^2)(9x^2 + 4y^2) = (3x-2y)(3x+2y)(9x^2 + 4y^2)$

3. The shaded region represents a picture frame. Find an expression for the area of the shaded region in simplest form.



$A_{\text{SHADED}} = A_{\text{LG}} - A_{\text{SM}}$

$A_{\text{LG}} = L \times W$
 $= (3x+4)(4x+3)$
 $= 12x^2 + 9x + 16x + 12$
 $= 12x^2 + 25x + 12$

$A_{\text{SM}} = L \times W$
 $= (x+1)(2x+1)$
 $= 2x^2 + x + 2x + 1$
 $= 2x^2 + 3x + 1$

$A_{\text{SHADED}} = (12x^2 + 25x + 12) - (2x^2 + 3x + 1)$
 $= 12x^2 + 25x + 12 - 2x^2 - 3x - 1$
 $= 10x^2 + 22x + 11$